

day 21

3.1/63 $f(x) = \begin{cases} 2x^2 & , x \leq 1 \\ ax-2 & , x > 1 \end{cases}$

Given $f(x)$ is continuous at $x=1$

- $f(1)$ exists

- $\lim_{x \rightarrow 1} f(x) = 2$ $\lim_{x \rightarrow 1^+} f(x) = \lim_{x \rightarrow 1^+} ax-2 = (a-2)$

$\lim_{x \rightarrow 1^-} f(x) = \lim_{x \rightarrow 1^-} 2x^2 = 2$

$a-2=2; a=4$

$\lim_{x \rightarrow 1} f(x)$ exists ONLY when $a=4$

- $f(1) = 2 = \lim_{x \rightarrow 1} f(x)$

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day 21

$$\lim_{h \rightarrow 0} \frac{\sqrt{2+h} - \sqrt{2}}{h}$$

If this is a derivative $f'(a)$,
what is $f(x)$ and
what is a ?

$$f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

$$f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$$

$$f(x) = \sqrt{x}$$

$$a = 2$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

3.2/17 explain why or why not.

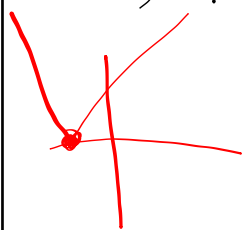
day 21

a) if the function is differentiable for all x ,
 then f is continuous for all x .

theorem
TRUE

+ left-diff and right-diff
 A function $f(x)$ is differentiable on an open interval (a,b) iff $f(x)$ has a derivative at every x in (a,b) .

b) The function $f(x) = |x+1|$ is continuous for all x , but not differentiable for all x



$$|?| = 0$$

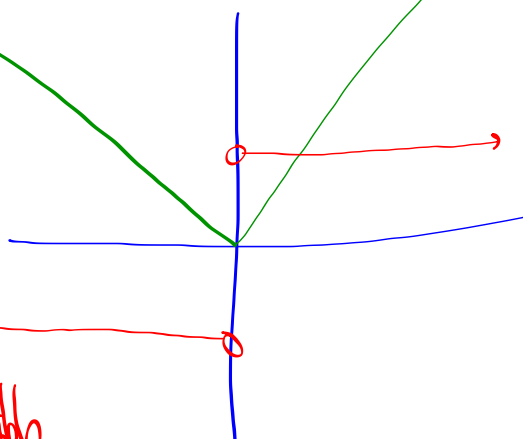
↑
0

so ricochet happens
 when
 $x+1=0$

$$\lim_{x \rightarrow -1} f'(x) \text{ DNE}$$

$f(x)$ is
continuous

$f(x)$ is
differentiable



$f(x)$ = differentiable
 on $(-\infty, 0)$
 and on
 $(0, \infty)$

and Not
 differentiable at
 $x = 0$

day 21

3.2
17c

It is possible for the domain of f to be (a, b) and the domain of f' to be $[a, b]$

Left what would it mean to be differentiable at $x=a$?

If $f'(x)$ is differentiable at a , then it would HAVE to be continuous at a .

$f(x)$ is diff at $x=a$ iff

$$\lim_{x \rightarrow a^+} \frac{f(x) - f(a)}{x - a} \text{ exists.}$$

"contradiction"

RIGHT

3.2/21 Find an equation of the normal line day 21

$$y = 3x - 4; P = (1, -1)$$

slope of tangent line = 3

slope of line perpendicular
to this is $-\frac{1}{3}$

$$Pt = (1, -1)$$

so

$$y - (-1) = -\frac{1}{3}(x - 1)$$